Name:\_\_\_\_\_

## §12.9 LAGRANGE MULTIPLIERS

1. Use Lagrange multipliers to find the closest point on the curve  $y = x^2$  to the point (0, 2).

2. Use Lagrange multipliers to find the maximum and minimum of the function f(x, y) = 4xy subject to the constraint  $4x^2 + y^2 = 8$ .

**3.** Find the maximum and minimum of the function f(x, y) = 4xy subject to the constraint  $4x^2 + y^2 \le 8$ .

4. Find the maximum and minimum of the function  $f(x,y) = 2x^3y$  subject to the constraint  $x^2 + y^2 \le 4$ .

5. Maximize  $f(x, y) = e^{x+y}$  subject to the constraint  $x^2 + y^2 = 2$ .

6. Minimize  $f(x, y, z) = x^2 + y^2 + z^2$  subject to the constraints x + 2y + 3z = 6 and y + z = 0.