Name:

## §12.9 Lagrange Multipliers

1. Use Lagrange multipliers to find the closest point on the curve $y=x^{2}$ to the point $(0,2)$.
2. Use Lagrange multipliers to find the maximum and minimum of the function $f(x, y)=4 x y$ subject to the constraint $4 x^{2}+y^{2}=8$.
3. Find the maximum and minimum of the function $f(x, y)=4 x y$ subject to the constraint $4 x^{2}+y^{2} \leq 8$.
4. Find the maximum and minimum of the function $f(x, y)=2 x^{3} y$ subject to the constraint $x^{2}+y^{2} \leq 4$.
5. Maximize $f(x, y)=e^{x+y}$ subject to the constraint $x^{2}+y^{2}=2$.
6. Minimize $f(x, y, z)=x^{2}+y^{2}+z^{2}$ subject to the constraints $x+2 y+3 z=6$ and $y+z=0$.
